# Relationships between Water Wettability and

Ice Adhesion

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ABSTRACT Ice formation and accretion may hinder the operation of many systems critical to national infrastructure, including airplanes, power lines, windmills, ships, and telecommunications equipment. Yet despite the pervasiveness of the icing problem, the fundamentals of ice adhesion have received relatively little attention in the scientific literature and it is not widely understood which attributes must be tuned to systematically design "icephobic" surfaces that are resistant to icing. Here we probe the relationships between advancing/receding water contact angles and the strength of ice adhesion to bare steel and twenty-one different test coatings (~200-300 nm thick) applied to the nominally smooth steel discs. Contact angles are measured using a commercially available goniometer, whereas the average strengths of ice adhesion are evaluated with a custom-built laboratory-scale adhesion apparatus. The coatings investigated comprise commercially available polymers and fluorinated polyhedral oligomeric silsesquioxane (fluorodecyl POSS), a low-surface-energy additive known to enhance liquid repellency. Ice adhesion strength correlates strongly with the practical work of adhesion required to remove a liquid water drop from each test surface (i.e., with the quantity  $[1 + \cos \theta_{rec}]$ ), and the average strength of ice adhesion was reduced by as much as a factor of 4.2 when bare steel discs were coated with fluorodecyl POSS-containing materials. We argue that any further appreciable reduction in ice adhesion strength will require textured surfaces, as no known materials exhibit receding water contact angles on smooth/flat surfaces that are significantly above those reported here (i.e., the values of [1 +  $\cos \theta_{\rm rec}$ ] reported here have essentially reached a minimum for known materials).

**KEYWORDS:** ice adhesion • icephobic • contact angle • hydrophobic • water wettability • fluoro POSS

#### INTRODUCTION

■ he formation and accretion of ice on exposed surfaces may hinder the operational performance of, for example, aircraft (1-3), helicopters (2, 4), ships (2, 5), offshore oil platforms (6), power lines (2, 7), wind turbines (8, 9), locks and dams (2, 10), and telecommunications equipment (2, 11, 12). Often some sort of deicing protocol, such as spraying aircraft with glycol-based fluids (1, 13, 14), is used to mitigate complications due to icing by removing ice that has formed on a surface. Such processes are suboptimal, however, because they require frequent application (e.g., spraying a plane before each cold weather departure), may be expensive (10), and often have detrimental environmental consequences (1, 13, 14). A related strategy utilizes "sacrificial" coatings (e.g., silicone grease) that remove ice particulates as they are shed from treated surfaces (3, 15, 16). Although this approach has proven effective in reducing ice adhesion (3, 15, 16), these sacrificial coatings, similar to deicing protocols, may negatively impact the environment and require periodic reapplication, although some recently developed sol-gel systems that slowly

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release freezing point depressants may significantly reduce the required frequency of reapplication (17, 18). A more appealing and universal approach is to design surfaces to which ice minimally adheres, ideally such that the ice debonds under its own weight or due to natural factors such as wind. The elucidation of the mechanism(s) of ice adhesion and the requisite surface properties to minimize ice-substrate interactions should facilitate the successful development of such "icephobic" coatings. Researchers have pursued such an understanding for more than 50 years, greatly increasing knowledge of ice adhesion phenomena (2, 3, 5, 7, 8, 10-12, 19-58). A few of these earlier publications include extensive discussion of the previous literature detailing the relationships between ice adhesion and water wettability (2, 34), a focus of this manuscript. Yet despite these research efforts, clearly defined design principles for the preparation of icephobic surfaces have remained elusive.

A common theme in ice adhesion research has been the comparison of ice adhesion strength and water wettability (surface hydrophobicity). The surface energy characteristics of water and ice are comparable (59), indicating such an analysis is reasonable. Often, this comparison has taken the form of a plot or tabular listing of measured ice adhesion strength as a function of the "water contact angle" (23-25, 31, 34, 42, 43, 51, 53). Data presented in this manner do not always follow a common trend, however; some groups have reported that ice adhesion decreases with increasing water contact angle (34, 43, 51), whereas others have found

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little relation between the two parameters (23–25, 31, 53). Petrenko and Whitworth compiled ice adhesion and water contact angle data from several research groups on a single plot and found that, although the ice adhesion strength generally decreased with increasing water contact angle, significant scatter was present in the data; reported ice adhesion strengths varied by as much as a factor of 10 for some samples with comparable water contact angles (42).

We believe the lack of clear trends in these data derives from the use of a single, presumably static equilibrium, water contact angle as a quantitative measure of the water wettability. A number of groups have pointed out that a single contact angle does not adequately characterize the wettability of a surface as, for example, the angle of tilt required to induce sliding of sessile liquid drops does not correlate with any one contact angle (31, 60–62). Gao and McCarthy noted that a more complete description of liquid wettability (or conversely, repellency) could be provided by separately considering shear and tensile phenomena (61, 62). Drop sliding is inherently a shearing process; the minimum angle of tilt ( $\alpha$ ) at which a sessile droplet will spontaneously move can be predicted using an equation proposed by Furmidge (63)

$$(mg/w)\sin(\alpha) = \gamma_{LV}(\cos\theta_{rec} - \cos\theta_{adv})$$
 (1)

where m is the mass of the drop, g is the gravitational constant, w is the width of the drop perpendicular to the drop sliding direction,  $\gamma_{\rm LV}$  is the liquid—vapor surface tension of the liquid, and  $\theta_{\rm rec}$  and  $\theta_{\rm adv}$  are the receding and advancing contact angles of the liquid on the substrate, respectively. The dimensionless solid—liquid interaction parameter that correlates with  $\alpha$  is the contact angle hysteresis (CAH) in the form [ $\cos\theta_{\rm rec}-\cos\theta_{\rm adv}$ ], not any single contact angle value (61, 62).

The wettability (or repellency) of a substrate can alternatively be viewed from a thermodynamic viewpoint that considers the free energies associated with the formation and elimination of interfacial areas. The equilibrium work of adhesion ( $W_e$ ) is the reversible free energy associated with the creation and destruction of interfaces (64). For the case of liquid drops on solid surfaces,  $W_e$  can be calculated using the Young—Dupré equation:

$$W_{\rm e} = \gamma_{LV} (1 + \cos \theta_{\rm e}) \tag{2}$$

where  $\theta_{\rm e}$  is the equilibrium (Young's) contact angle (64–67). The solid—liquid interaction parameter that directly correlates with  $W_{\rm e}$  is the dimensionless factor [1 + cos  $\theta_{\rm e}$ ]. Many other terms are used in the literature to describe  $W_{\rm e}$ , including "fundamental work of adhesion" (68, 69), "thermodynamic work of adhesion" (68), "basic work of adhesion" (68), and more generically, "work of adhesion" (30, 31, 67). The idealized Young—Dupré equation may not, in practice, describe typical processes. For instance, the forces required to remove Wilhelmy plates from liquids (64, 67) or to separate surfaces connected by a capillary

bridge of water (70) are governed by the receding contact angle  $\theta_{\text{rec}}$ . It was on the basis of this latter result (70) that Gao and McCarthy suggested (61, 62) that the work of adhesion could be quantified using

$$W_{\rm p} = \gamma_{LV} (1 + \cos \theta_{\rm rec}) \tag{3}$$

Here we will use Mittal's terminology (68) and refer to  $W_p$  as the "practical work of adhesion" because it involves the actual work required to separate a liquid from a surface. The solid—liquid interaction parameter that directly scales with  $W_p$  is the quantity  $[1 + \cos \theta_{rec}]$  and, since  $[1 + \cos \theta_{rec}]$  is always larger than  $[1 + \cos \theta_e]$ ,  $W_p$  is always larger than  $W_e$ .

Ice adhesion strength may correlate more strongly with "water wettability" when "water wettability" is defined with respect to the shear and/or tensile processes described above. It is not obvious a priori which, if any, of the scaling relationships presented in eqs 1-3 should correlate with the strength of ice adhesion. All of these proposed correlations require water contact angles to be reflective of ice-substrate interactions, a reasonable hypothesis given the similarities in the surface energy characteristics of water and ice (59). The plausibility of this assumption will later be further examined using our water contact angle and ice adhesion strength data. A correlation with [ $\cos \theta_{
m rec} - \cos \theta_{
m adv}$ ] may be reasonable if an interfacial liquidlike layer, which has been proposed for ice adhered to substrates (20, 21, 71), promotes sliding of the interface prior to detachment of the ice column. It is also conceivable that ice adhesion strength scales with either  $W_e$  or  $W_p$ , as the adhesive detachment of ice from a substrate creates ice-vapor and substrate-vapor interfaces while destroying the ice-substrate interface.

Previously published data enable us to examine preliminarily the feasibility of these potential correlations. Murase and co-workers plotted the ice adhesion strength as a function of  $W_e$  for 22 different polymeric coatings (30, 31). Generally the measured ice adhesion strengths were lower for samples with lower  $W_e$ , although significant scatter was present in the data; for example, ice adhesion strengths of 1000 and 330 kPa were reported for samples with comparable W<sub>e</sub>. Kulinich and Farzaneh reported an approximately linear correlation between average strength of ice adhesion and water CAH in the form CAH =  $[\theta_{adv} - \theta_{rec}]$  for ten fluoropolymer/nanopowder coatings (53). The "water contact angles" (presumably advancing values) reported by Kulinich and Farzaneh for their samples only vary by  $\sim 13^{\circ}$ and most of the differences in CAH between surfaces are, therefore, the result of variations in  $\theta_{\rm rec}$  due to water droplets being in either the fully wetted Wenzel (72) (low  $\theta_{\rm rec}$ ) or the composite Cassie-Baxter (73) (high  $\theta_{rec}$ ) state (53). Consequently, plots of the ice adhesion strength versus the scaling parameter [1 +  $\cos \theta_{\rm rec}$ ] would also be approximately linear, consistent with a correlation between the ice adhesion strength and the practical work of adhesion of water  $W_p$ . Raraty and Tabor (19) reported ice adhesion strengths and receding water contact angles on four different flat organic substrates. These ice adhesion strengths (19), like those on

surfaces studied by Kulinich and Farzaneh (53), varied approximately linearly with the dimensionless parameter [1 +  $\cos\theta_{\rm rec}$ ] evaluated for water, consistent with practical work of adhesion of water playing a key role in ice adhesion. While it is not possible to reach definitive conclusions given the limited amount of data reported in the literature, it does appear that ice adhesion strength correlates more strongly with either the roll-off angle for water drops or the practical work of adhesion of water than it does with static water contact angles.

In this work, we examine the relationships between water wettability and ice adhesion strength on nominally smooth bare and coated steel discs. The Wenzel roughness for these surfaces (i.e., the actual surface area/occluded surface area) is r < 1.01. Twenty-one different test coatings with a broad range of substrate-water interactions were employed, including commercially available polymers such as Tecnoflon (a fluoroelastomer), poly(ethyl methacrylate) (PEMA), poly-(methyl methacrylate) (PMMA), poly(butyl methacrylate) (PBMA), polycarbonate (PC), and cross-linked poly(dimethyl siloxane) (PDMS), as well as (1H,1H,2H,2H-heptadecafluorodecyl)<sub>8</sub>Si<sub>8</sub>O<sub>12</sub>, or fluorodecyl polyhedral oligomeric silsesquioxane (fluorodecyl POSS), and blends of Tecnoflon or PEMA with fluorodecyl POSS. Fluorodecyl POSS is a very low surface energy material ( $\gamma_{SV} \approx 10$  mN/m) (74) that has been used to prepare a variety of water and oil repellent surfaces (74–79), and solution blending provides a means of tuning the surface wettability of polymeric films/coatings cast from solution. For our samples, the average strength of ice adhesion varies nearly linearly with the interaction parameter [1 +  $\cos \theta_{\rm rec}$ ] that scales with the practical work of adhesion  $(W_p)$  for liquid water. This result suggests that maximizing the receding water contact angle  $\theta_{\rm rec}$  minimizes ice adhesion.

### **EXPERIMENTAL SECTION**

Materials. Asahiklin (AK225, Asahi Glass Company) and dichloromethane (Aldrich) solvents were used as received. Tecnoflon (Solvay Solexis), PEMA (Aldrich,  $M_w = 515 \text{ kg/mol}$ ), PMMA (Scientific Polymer Products,  $M_w = 540 \text{ kg/mol}$ ), PBMA (Aldrich,  $M_w = 337 \text{ kg/mol}$ ), and PC (Bayer) polymers were used as received. PDMS (Sylgard 184) was generously provided as a kit by Dow Corning; the base and curing agent were dissolved in Asahiklin in a 10:1 (by weight) ratio, spin-coated onto steel discs, and heated for ~2 h at 60 °C to cross-link the chains. Fluorodecyl POSS was prepared following established protocols (75). Steel discs were purchased from Mary-o-lus Manufacturing and were soaked in acetone and dried under an air purge prior to use. These discs are 25 mm in diameter, 1.5 mm thick, have a measured root-mean square roughness ( $R_0$ ) = 0.9  $\pm$  0.2  $\mu$ m, and a measured Wenzel roughness (i.e., the actual surface area/ occluded surface area) r < 1.01.

Coating Methodology. Solutions (total solids 20 mg/mL) were prepared by dissolving both the polymers and the fluorodecyl POSS in Asahiklin. Dichloromethane was used to prepare the PC solution because PC is not soluble in Asahiklin. Thin ( $\sim\!200-300$  nm) coatings were deposited at room temperature on the steel discs via a spin coating process;  $\sim\!0.2$  mL of solution was placed on top of each disk and the disk was spun at 900 rpm for 30 s.

**Surface Characterization.** The roughness of representative test substrates was measured using a Zygo interferometer and

a Mitutoyo Surftest SJ-210 contact profilometer equipped with a 10  $\mu$ m diameter stylus. A topographical depiction of a bare steel disc surface and measured roughness parameters for all 22 test substrates are provided in Figure S1 and Table S1 in the Supporting Information. Scanning electron microscopy (SEM) images were acquired using a JEOL 6060 instrument operating at an acceleration voltage of 5 kV. Atomic force microscopy (AFM) measurements were carried out using a Veeco Metrology Group Dimension 3100 instrument operating in the tapping mode. X-ray photoelectron spectroscopy (XPS) was performed using a Kratos Axis Ultra X-ray photoelectron spectrometer manufactured by Kratos Analytical (Manchester, England). The monochromatized Al K $\alpha$  source was operated at 15 kV and 10 mA (150 W) and emissions were collected at takeoff angles of 90° relative to the sample surface. Contact angles of deionized water (18 M $\Omega$ -cm, Millipore) on test surfaces were measured using a VCA2000 goniometer (AST Inc.). Advancing ( $\theta_{adv}$ ) and receding ( $\theta_{\rm rec}$ ) angles were measured as water was supplied via a syringe into or out of sessile droplets (drop volume  $\sim$ 5  $\mu$ L).

Ice Adhesion Measurements. While goniometers are widely used to measure liquid contact angles, there are no analogous, readily available commercial instruments designed to measure solid-solid (e.g., ice-substrate) adhesion strengths. A few groups have deposited glaze ice by spraying supercooled water droplets over test substrates and then measured the average strength of ice adhesion using a centrifuge apparatus (51-55, 57, 58). Although this setup is designed to mimic the environmental icing conditions encountered by, for example, power lines subject to freezing rain or airplanes colliding with supercooled water droplets in the atmosphere, it is not practical for most academic laboratories because it requires an icing chamber and complex centrifuge setup. A number of other groups have used simpler apparatus that involve pouring liquid water onto a test substrate, freezing the water, and then measuring the average stress required to remove the ice from the test surface (12, 19, 23-25, 27, 30, 31, 34, 35, 43). We designed and constructed an adhesion test apparatus broadly following the physical principles of this latter strategy. Water columns were frozen to coated steel discs using the protocol summarized schematically in Figure 1 and described below. Coated steel discs were first clamped to a custom-built base plate (4  $\times$  5 array). Deionized water (1.5 mL) was syringed into 20 glass cuvettes (1 cm  $\times$  1 cm  $\times$  4.4 cm, Scientific Equipment of Houston) that had been modified by: (1) polishing the tops of the open ends using a Buehler EcoMet 250/300 Grinder-Polisher equipped with 1200 grit sandpaper; (2) treating the cuvettes with 1H,1H,2H,2H-perfluorodecyltrichlorosilane (Gelest) vapor to reduce their surface energies. These modified cuvettes were then loaded into a custom-built sample holder ( $4 \times 5$  array). The base plate was inverted and placed on top of the sample holder, and this assembly was bolted together to provide flush contact between the cuvettes and test substrates. Water typically did not leak from the inverted cuvettes provided the glass had been polished to enhance the physical contact with the test substrate and treated with 1H,1H,2H,2H-perfluorodecyltrichlorosilane to reduce its surface energy and water wettability. This assembly was mounted on top of a liquid-cooled Peltier cooling plate (TECA Corporation, model LHP-800CP) that was housed in a low-humidity nitrogen atmosphere to minimize frost formation on the samples and test apparatus. The temperature of the cooling plate surface was monitored using a thermocouple washer bolted to the top of the plate, and the test specimens were cooled at a rate of ~2 °C/min to the target temperature (typically -10 °C to facilitate comparison with previously reported data (51, 53)). The water was frozen overnight ( $\sim$ 10-15 h) and the sample holder was carefully removed from the assembly, leaving ice columns encased in cuvettes and adhered to the test substrates. The force required

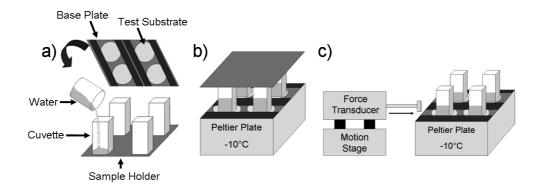


FIGURE 1. Schematic depiction of the procedure used to freeze water columns on test substrates and to measure the ice adhesion strength. The actual apparatus can hold a  $4 \times 5$  array of samples; a  $2 \times 2$  array is used here for ease of illustration. (a) Deionized water is poured into cuvettes housed in a sample holder (bottom) and coated steel discs are clamped onto a base plate (top). The samples attached to the base plate are then mounted flush against the tops of the cuvettes. (b) The base plate-sample holder assembly is taken into a glovebox operating under a nitrogen atmosphere, inverted, and bolted to a Peltier cooling plate whose surface is thermostatted at a target temperature (-10 °C unless otherwise specified). An insulating foam box is placed over the assembly to reduce the cooling load required of the chiller and the water columns are allowed to freeze for 10-15 h. (c) The top sample holder is removed and the probe of a force transducer is propelled at 0.5 mm/s, unless otherwise specified, into the side of each cuvette until the ice detaches from the test surface. The maximum force is recorded and converted into ice adhesion strength using the known cross-sectional area of the ice-substrate interface.

to detach each ice column from its test substrate was measured by propelling the 0.8 cm diameter probe of a force transducer (Imada, model ZP-44) into the side of the cuvette at a constant velocity of 0.5 mm/s unless otherwise specified. The probe velocity was controlled using a motion stage (MICOS, model VT80). The probe was located less than 2 mm above the substrate surface to minimize torque on the ice sample. The measured maximum force at break was converted into ice adhesion strength by dividing by the known cross-sectional area (1 cm²) of the ice—substrate interface. A photograph of the assembled apparatus in operation is provided in Figure S2 in the Supporting Information.

## **RESULTS AND DISCUSSION**

Water contact angle and ice adhesion measurements (-10 °C, 0.5 mm/s probe velocity) for the 22 tested surfaces are summarized in Table 1. Notably, the magnitudes of the measured ice adhesion strengths (165-510 kPa) are comparable to those reported in the literature for textured surfaces using a centrifuge setup (50-500 kPa) (51-55), evidence that the apparatus described in Figure 1 yields quantitatively meaningful data. Each test coating was applied to at least four different steel discs, one of which was a control that was not subjected to icing conditions. Water contact angles were measured before and after each ice adhesion measurement to probe the durability of the coatings. Contact angles measured on the tested substrates were within the experimental uncertainties of those measured on the control surfaces, indicating the (typically 3-5) ice adhesion tests did not damage or remove the deposited coatings. Generally, the removal of ice from test surfaces was adhesive in nature, with no residual ice visible on the coating following testing. In some cases, however, mixed-mode (68) failure was observed, with some shards of ice (<25% of the ice—substrate interfacial area) remaining adhered to the test substrate following detachment of the macroscopic ice column. The probability of a mixed-mode failure generally increased as the receding water contact angle  $\theta_{\rm rec}$  decreased, as can be seen upon examination of the fractions of tests with completely adhesive failure (i.e., no ice shards remaining on the substrate) that are provided in Table 1. The measured ice adhesion strengths did not significantly vary for these two failure modes, and data from both subpopulations are included in the average ice adhesion strengths reported in Table 1.

The measured average strengths of ice adhesion are plotted against two different measures of the water contact angle in Figure 2 to allow for ready comparison with previous literature (23-25, 31, 34, 42, 43, 51, 53). It is difficult to measure equilibrium static water contact angles because droplets can adopt long-lived metastable configurations with an instantaneous contact angle anywhere between  $heta_{ ext{adv}}$  and  $\theta_{\rm rec}$  (62, 80). As an alternative, two values were chosen that are believed to provide plausible bounds for the equilibrium contact angle. The advancing contact angle  $\theta_{\text{adv}}$ , which some have used as an approximation of  $\theta_e$  (81), is used as the abscissa in Figure 2a. Other groups have suggested that equilibrium-like contact angles can be obtained by vibrating liquid drops (81-83). All of these vibrated drops, regardless of initial position, consistently adopted a final configuration with a unique contact angle between  $heta_{
m adv}$  and  $heta_{
m rec}$ . This angle  $\theta_{\rm e}$  can be estimated (81–83) from  $\theta_{\rm adv}$  and  $\theta_{\rm rec}$  measurements using

$$\cos \bar{\theta}_{e} = 0.5(\cos \theta_{adv} + \cos \theta_{rec}) \tag{4}$$

Measurements of the advancing and receding contact angles  $\theta_{adv}$  and  $\theta_{rec}$  are reproducible (62), enabling consistent estimation of  $\bar{\theta}_e$ . Static contact angles measured using typical goniometric techniques are higher than  $\bar{\theta}_e$  (81), leading to the selection of  $\bar{\theta}_e$  as a lower bound for single water contact angle measurements and as the abscissa in Figure 2b. The curves in panels a and b in Figure 2 both generally have a negative slope, consistent with some literature reports that ice adhesion decreases with increasing water contact angle (34, 42, 43, 51). There is less scatter present when  $\bar{\theta}_e$  is used

Table 1. Measured Water Contact Angles and Average Strengths of Ice Adhesion for the 22 Tested Surfaces

substrate	$ heta_{ ext{adv}}$ , water $^a$	$ heta_{ m rec}$ , water $^a$	no. of ice adhesion tests	fraction of tests with complete adhesive failure <sup>b</sup>	average strength of ice adhesion at $-10$ °C (kPa) <sup>c</sup>
bare steel	86.2 ± 3.3	$25.8 \pm 2.5$	9	0.33	698 ± 112
PMMA	$83.6 \pm 3.6$	$60.7 \pm 1.3$	11	0.73	$463 \pm 65$
PC	$93.4 \pm 1.0$	$73.9 \pm 3.3$	7	0.86	$400 \pm 83$
PBMA	$92.8 \pm 2.4$	$74.6 \pm 1.7$	9	0.44	$384 \pm 52$
PDMS (Sylgard 184)	$108.9 \pm 1.5$	$91.7 \pm 5.1$	9	1.00	$291 \pm 44$
PEMA	$84.6 \pm 2.4$	$68.0 \pm 2.5$	9	0.67	$510 \pm 101$
99/1 PEMA/fluorodecyl POSS	$97.5 \pm 2.2$	$67.5 \pm 2.2$	9	0.22	$475 \pm 50$
97/3 PEMA/fluorodecyl POSS	$105.4 \pm 3.7$	$77.0 \pm 4.7$	8	1.00	$367 \pm 86$
95/5 PEMA/fluorodecyl POSS	$122.2 \pm 2.0$	$104.0 \pm 5.3$	8	1.00	$278 \pm 93$
90/10 PEMA/fluorodecyl POSS	$122.6 \pm 2.1$	$107.6 \pm 6.9$	12	0.92	$247 \pm 45$
80/20 PEMA/fluorodecyl POSS	$123.8 \pm 1.2$	$118.2 \pm 2.4$	7	1.00	$165 \pm 27$
70/30 PEMA/fluorodecyl POSS	$124.2 \pm 0.9$	$116.4 \pm 2.9$	9	1.00	$166 \pm 44$
50/50 PEMA/fluorodecyl POSS	$125.0 \pm 1.7$	$114.1 \pm 2.4$	8	1.00	$185 \pm 57$
Tecnoflon	$118.3 \pm 1.4$	$73.7 \pm 2.1$	17	0.76	$389 \pm 63$
99/1 Tecnoflon/fluorodecyl POSS	$125.7 \pm 1.9$	$79.2 \pm 3.4$	13	0.92	$392 \pm 88$
97/3 Tecnoflon/fluorodecyl POSS	$127.0 \pm 1.7$	$87.7 \pm 4.8$	11	0.82	$412 \pm 64$
95/5 Tecnoflon/fluorodecyl POSS	$126.6 \pm 1.2$	$92.9 \pm 4.3$	15	1.00	$328 \pm 97$
90/10 Tecnoflon/fluorodecyl POSS	$126.6 \pm 0.8$	$98.0 \pm 5.3$	9	1.00	$345 \pm 104$
80/20 Tecnoflon/fluorodecyl POSS	$126.0 \pm 0.9$	$103.7 \pm 4.3$	11	1.00	$313 \pm 70$
70/30 Tecnoflon/fluorodecyl POSS	$125.2 \pm 0.8$	$110.0 \pm 3.1$	9	1.00	$205 \pm 40$
50/50 Tecnoflon/fluorodecyl POSS	$128.3 \pm 1.1$	$108.7 \pm 3.4$	8	1.00	$265 \pm 42$
fluorodecyl POSS	$137.6 \pm 4.8$	$110.0 \pm 3.8$	15	1.00	$250 \pm 54$

 $<sup>^</sup>a$  Uncertainties are standard deviations in all data collected before and after ice adhesion tests.  $^b$  Mixed-mode (68) failures with small shards of ice remaining adhered to test substrates were observed for some samples.  $^c$  The force probe impacted the cuvette-encased ice columns at a velocity of 0.5 mm/s, and uncertainties are computed using a Student's t test with 95% confidence intervals.

as the abscissa (for a linear fit, the square of the correlation coefficient is  $R^2 = 0.82$ ) than when  $\theta_{\rm adv}$  (for a linear fit,  $R^2 = 0.54$ ) is selected.

The concepts of shear and tensile wettability (eqs 1-3), which require measurements of  $\theta_{\rm adv}$  and  $\theta_{\rm rec}$ , can be used to describe solid-liquid interactions more accurately and completely than any single contact angle value (61, 62). Our data can be used to test the applicability of this wettability framework to substrate-ice adhesion. We begin our examination of the applicability of the shear and tensile adhesion framework for water to ice-substrate adhesion strengths with a comparison of the ice adhesion strength and the water CAH parameter [ $\cos heta_{
m rec} - \cos heta_{
m adv}$ ] that scales with liquid drop roll-off angle (see eq 1). This interaction parameter could plausibly influence ice adhesion strength if the interface between ice and a substrate is comprised of a liquidlike layer, as has been proposed (20, 21, 71); such a liquidlike interface could facilitate lateral sliding prior to detachment of the ice column. The measured ice adhesion strengths are plotted in Figure 3 against the CAH parameter [cos  $\theta_{\rm rec}$  - cos  $\theta_{\rm adv}$ ], which scales with liquid drop roll-off angle (see eq 1). Data acquired from hydrophobic test substrates with  $\theta_{adv} > 105^{\circ}$  correlate almost linearly ( $R^2 =$ 0.86) with [cos  $\theta_{\rm rec}$  - cos  $\theta_{\rm adv}$ ], a result consistent with Kulinich and Farzaneh's measurements of the strength of ice adhesion to rough fluoropolymer/nanopowder coatings (53). Kulinich and Farzaneh used CAH =  $[\theta_{adv} - \theta_{rec}]$  as the abscissa, whereas we are utilizing the [cos  $heta_{
m rec}$  - cos  $heta_{
m adv}$ ] scaling parameter that appears in eq 1. The differences in the plot shapes are relatively minor for our data, as can be seen from a comparison of Figure 3 and Figure S3 in the Supporting Information. Notably, and unlike the data of Kulinich and Farzaneh (53), our data set contains numerous points that deviate significantly from this nearly linear trend. The six samples with  $\theta_{\rm adv}$  < 100° adhere to ice more strongly than anticipated based upon the linear best fit of the ice adhesion strength versus [cos  $\theta_{\text{rec}}$  - cos  $\theta_{\text{adv}}$ ], providing compelling evidence that ice adhesion strength does not always correlate linearly with water CAH. Further evidence that  $[\cos \theta_{\rm rec} - \cos \theta_{\rm adv}]$  is not the proper scaling factor for ice adhesion strength comes from extrapolations of the linear fits to both our and Kulinich and Farzaneh's data (53). In neither case does a plausible linear fit pass through the origin, suggesting that even as  $[\cos \theta_{\rm rec} - \cos \theta_{\rm adv}] \rightarrow 0$ , ice will still adhere to substrates; presumably the strength of ice adhesion will approach zero when the correct correlation analysis is applied.

Ice adhesion strength is next considered in the context of tensile phenomena for liquid water. Average strengths of ice adhesion are presented in Figure 4 as functions of parameters that scale with the equilibrium (1 + cos  $\bar{\theta}_{e}$ , Figure 4a) and practical (1 + cos  $\theta_{rec}$ , Figure 4b) works of adhesion for water on these same surfaces. We believe that the average strength of ice adhesion should approach zero along with the governing interaction parameter, and, consequently, the data were fit with the constraint that the linear correlations pass through the origin. The solid/dashed lines depicted in Figure 4 are these best fits (with the dashed

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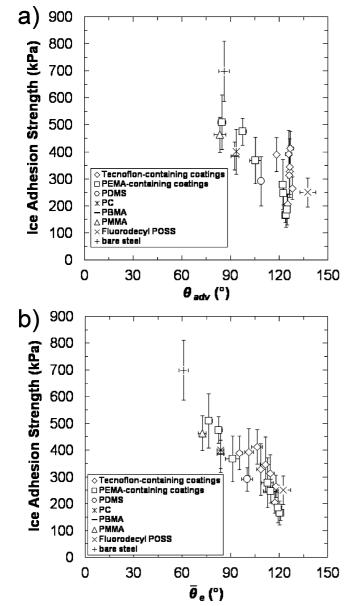


FIGURE 2. Average strengths of ice adhesion measured at  $-10\ ^{\circ}\text{C}$ for bare steel and 21 different coatings and plotted against two different measured water contact angles:(a) the advancing water contact angle  $\theta_{adv}$  and (b) the estimated equilibrium contact angle  $\bar{\theta}_{\rm e}$  computed using the proposed (60, 81–83) approximation given in eq 4. Static water contact angles reported in the literature likely fall between  $\theta_{\rm adv}$  and  $\bar{\theta}_{\rm e}$  (81), and these plots facilitate comparison with previous presentations of ice adhesion measurements (23-25, 31, 34, 42, 43, 51, 53).

portions representing the extrapolation to the origin). The best fit correlation ( $R^2 = 0.92$ , Figure 4b) between ice adhesion strength and [1 +  $\cos \theta_{
m rec}$ ] yields the following expression for the average strength of ice adhesion

$$\tau_{\rm ice} = (340 \pm 40 \text{ kPa})(1 + \cos \theta_{\rm rec})$$
 (5)

This correlation is significantly stronger than the correlation with  $[1 + \cos \bar{\theta}_e]$  ( $R^2 = 0.80$ , Figure 4a). The linearity of the data depicted in Figure 4b is consistent with the earlier assumption that water contact angles are reflective of ice-substrate interactions. Furthermore, the correlation

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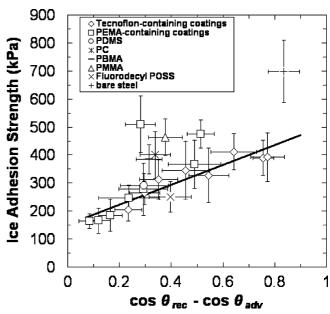


FIGURE 3. Average strengths of ice adhesion measured at -10 °C for bare steel and 21 different coatings plotted against a measure of water contact angle hysteresis which scales with liquid drop rolloff angle (see eq 1). The solid line is the linear best fit to the data acquired from the 16 surfaces with  $\theta_{adv} > 105^{\circ}$ .

with  $[1 + \cos \theta_{\rm rec}]$  improves only slightly ( $R^2$  increases by < 0.001) when the linear best fit is not required to pass through the origin, supporting the hypothesis that the average strength of ice adhesion should approach zero along with the correct scaling parameter. This correlation with  $[1 + \cos \theta_{\rm rec}]$  is also stronger than Murase et al.'s proposed relationship between the ice adhesion strength and the equilibrium work of adhesion for water computed using Bangham and Razouk's modification (84) of eq 2 that incorporates a reduction in solid surface energy due to adsorption of water vapor (30, 31).

The validity of the proposed scaling between ice adhesion strength and [1 +  $\cos heta_{
m rec}$ ] is further supported by Kulinich and Farzaneh's data (53), which are replotted against  $[1 + \cos \theta_{\rm rec}]$  in Figure S4 in the Supporting Information. For this plot, receding water contact angles  $heta_{
m rec}$  were calculated using the reported CAH and the assumption that the "water contact angles" listed in the paper (53) were advancing values. The scaling argument that the ice adhesion strength should be zero when the practical work of adhesion for water is zero was again used to require the linear best fit to pass through the origin. The high correlation coefficient for this linear best fit of the Kulinich and Farzaneh data (53)  $(R^2 = 0.93$ , see Figure S4 in the Supporting Information) is further support for our proposal that the measured strength of ice adhesion depends on the magnitude of the liquid water parameter [1 +  $\cos \theta_{\rm rec}$ ] which is measured on the solid surface under consideration.

The sensitivities of the measured average strengths of ice adhesion to variations in temperature and the speed of the incident force transducer were probed for four test substrates that span a broad range of receding water contact angle values: 80/20 PEMA/fluorodecyl POSS ( $\theta_{rec} = 118.2^{\circ}$  $\pm$  2.4°), 90/10 PEMA/fluorodecyl POSS ( $\theta_{\rm rec} =$  107.6°  $\pm$ 

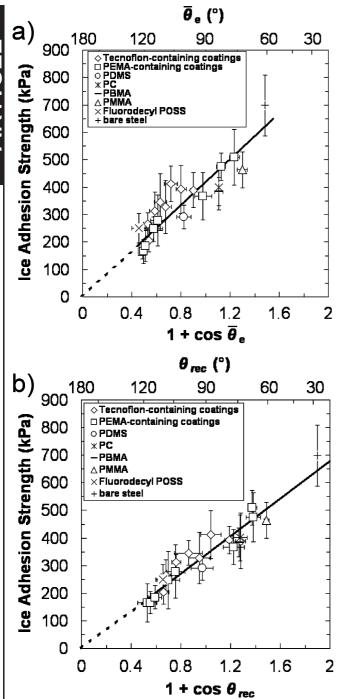


FIGURE 4. Average strengths of ice adhesion measured at -10 °C for bare steel and 21 different coatings plotted against water contact angle parameters that scale with (a) the equilibrium work of adhesion for liquid water (see eq 2) and (b) the practical work of adhesion for liquid water (see eq 3). The straight lines are the linear best fits that pass through each origin, with the solid portions of the lines encompassing the measured data and the dashed portions representing the extrapolation to the origin. The linear fit for (b) ( $\tau_{\rm ice} = (340 \pm 40 \ {\rm kPa})(1 + \cos\theta_{\rm rec}), R^2 = 0.92$ ) is significantly better than that for (a) ( $R^2 = 0.80$ ).

6.9°), PDMS (Sylgard 184) ( $\theta_{rec} = 91.7^{\circ} \pm 5.1^{\circ}$ ), and PBMA ( $\theta_{rec} = 74.6^{\circ} \pm 1.7^{\circ}$ ). These experimental results are summarized in Table 2 and in Figure S7 in the Supporting Information. The values of the average strength of ice adhesion for each set of test conditions were plotted against [1 +  $\cos \theta_{rec}$ ] and linear best fits through each origin were

obtained and are reported in Table 3. These linear fits depend on data from all four test substrates and provide a quantitative means of comparing the ensembles of data collected at the five different test conditions. The slopes of the fits to the data acquired at various probe displacement speeds at -10 °C are clearly not statistically different, indicating that the stress of ice detachment is not sensitive to the incident probe speed over this range (0.1-1.5 mm/s). Although the best fit slope of the -5 °C data is larger than those obtained by fitting the -10 and -15 °C data, statistical analysis using Student's t test with 95 % confidence intervals reveals that there is only a 45% chance that the highest and lowest slopes of the fits (obtained from the -5 and -15 °C data) are in fact different, too small of a probability to draw any firm conclusions. Raraty and Tabor (19) and Landy and Freiberger (24) similarly reported that ice adhesion strength is not sensitive to substrate temperature over this -5 to -15 °C range provided the mode of interfacial failure is adhesive.

Although it is clearly economically desirable to minimize the amount of relatively expensive fluorodecyl POSS incorporated into coatings, examination of the data reported in Table 1 suggests that there are also performance benefits associated with "diluting" the fluorodecyl POSS with commercially available polymers. Water has the highest advancing contact angle  $heta_{adv}$  on pure fluorodecyl POSS, but does not exhibit the highest receding contact angle  $heta_{
m rec}$  on this fluorinated coating, and consequently, ice adheres to discs coated with pure fluorodecyl POSS ( $\theta_{\rm rec}$  = 110.0  $\pm$  3.8°,  $\tau_{\rm ice}$ = 250  $\pm$  54 kPa) more strongly than it does to discs coated with, for example, 80/20 PEMA/fluorodecyl POSS ( $\theta_{\rm rec} =$  $118.2 \pm 2.4$ °,  $\tau_{\rm ice} = 165 \pm 27$  kPa). The 80/20 PEMA/POSS surface was selected for comparison because of its combination of a low fluorodecyl POSS loading and a minimal adherence to ice. The relative water repellency and "icephobicity" of coatings are connected to the topographic structure of the surface of the deposited film. SEM and tapping-mode AFM were used to probe surface topographies of  $\sim$ 200-300 nm thick layers of pure fluorodecyl POSS and 80/20 PEMA/ fluorodecyl POSS that were deposited on silicon wafers by spin coating. The pure fluorodecyl POSS coatings are substantially rougher than the 80/20 PEMA/fluorodecyl POSS films in the SEM images presented in Figure S8. This observation was confirmed by AFM height measurements presented in Figure S9 that yielded a root-mean square roughness  $R_0 = 39$  nm and a Wenzel roughness r = 1.74for pure fluorodecyl POSS, and  $R_q = 2$  nm and r = 1.04 for the 80/20 PEMA/POSS coating. We believe that the increased roughness of the pure fluorodecyl POSS coating resulting from the spin coating process leads to a reduction in  $\theta_{\rm rec}$  (64) and the concomitant increase in ice adhesion strength compared to the smoother 80/20 PEMA/fluorodecyl POSS surface. Blending PEMA with fluorodecyl POSS is thus not only economically desirable but also improves coating performance by (i) facilitating the deposition of a smooth film with high fluorine content that exhibits maximum values of receding water contact angles; (ii) possibly enhancing me-

Table 2. Measured Receding Water Contact Angles and Average Strengths of Ice Adhesion for Four Test Substrates at Several Temperatures and Force Transducer Speeds

substrate coating	T (°C)	incident probe speed (mm/s)	$ heta_{ m rec}$ , water $^a$	no. of ice adhesion tests	fraction of tests with complete adhesive failure <sup>b</sup>	average strength of ice adhesion at -10 °C (kPa) <sup>c</sup>
80/20 PEMA/fluorodecyl POSS	-10	0.1	$118.2 \pm 2.4$	10	1.00	196 ± 38
	-10	0.5		7	1.00	$165 \pm 27$
	-10	1.5		10	1.00	$196 \pm 35$
	-5	0.5		8	1.00	$215 \pm 21$
	-15	0.5		10	0.90	$160 \pm 46$
90/10 PEMA/fluorodecyl POSS	-10	0.1	$107.6 \pm 6.9$	8	1.00	$227 \pm 54$
	-10	0.5		12	0.92	$247 \pm 45$
	-10	1.5		10	1.00	$234 \pm 59$
	-5	0.5		8	1.00	$297 \pm 47$
	-15	0.5		8	1.00	$220 \pm 52$
PDMS (Sylgard 184)	-10	0.1	$91.7 \pm 5.1$	8	1.00	$264 \pm 26$
	-10	0.5		9	1.00	$291 \pm 44$
	-10	1.5		7	1.00	$269 \pm 111$
	-5	0.5		8	0.88	$328 \pm 91$
	-15	0.5		6	1.00	$279 \pm 56$
РВМА	-10	0.1	$74.6 \pm 1.7$	8	0.75	$413 \pm 98$
	-10	0.5		9	0.44	$384 \pm 52$
	-10	1.5		8	0.50	$428 \pm 93$
	-5	0.5		7	0.63	$485 \pm 133$
	-15	0.5		9	0.22	$400 \pm 98$

<sup>&</sup>lt;sup>a</sup> Uncertainties are standard deviations in all of the data collected before and after ice adhesion tests. <sup>b</sup> Mixed-mode (68) failures with small shards of ice remaining adhered to test substrates were observed for some samples. <sup>c</sup> The uncertainties were calculated using a Student's *t* test with 95% confidence intervals.

Table 3. Linear Best Fits of Plots of Average Strengths of Ice Adhesion versus Receding Water Contact Angles at Several Temperatures and Incident Force Transducer Speeds

		incident probe speed		slope of linear best	
test condition	T (°C)	(mm/s)	no. of test substrates	fit <sup>a</sup> (kPa)	$R^2$ of linear best fit
1	-10	0.1	4	$314 \pm 133$	0.90
2	-10	0.5	$22^{b}$	$340 \pm 40$	0.92
2	-10	0.5	$4^c$	$311 \pm 84$	0.95
3	-10	1.5	4	$323 \pm 109$	0.90
4	-5	0.5	4	$378 \pm 125$	0.92
5	-15	0.5	4	$307 \pm 101$	0.98

<sup>&</sup>lt;sup>a</sup> Uncertainties were computed using a Student's *t* test with 95% confidence intervals. <sup>b</sup> Data from all 22 test substrates listed in Table 1 are used to calculate the fit. <sup>c</sup> Only data from 80/20 PEMA/fluorodecyl POSS, 90/10 PEMA/fluorodecyl POSS, PDMS (Sylgard 184), and PBMA test samples were used to compute the fit.

chanical properties of the film by incorporating a durable polymer binder into the coating.

The molecular and topographic structure of the 80/20 PEMA/fluorodecyl POSS film deposited on silicon were further probed using XPS and AFM phase imaging. Atomic ratios computed using the XPS survey spectra are 1.54 for F/C, 0.11 for O/C, and 0.09 for Si/C. These values are close to those expected for pure fluorodecyl POSS (1.7 for F/C, 0.15 for O/C, and 0.1 for Si/C) (78), indicative of a thermodynamically driven segregation or "blooming" (76) of the fluorodecyl POSS toward the surface. Additional information about the molecular composition of the surface can be gleaned from XPS by examining the high-resolution carbon 1s spectrum that is presented in Figure 5a. The peaks in this spectrum were indexed by comparing the measured binding energies at peak maxima with standard spectra available for PEMA and poly(vinylidene fluoride) (85). The peak associ-

ated with the  $-CF_2-$  moiety is roughly four times as intense as that associated with the  $-CH_2-$  moiety, further evidence that fluorodecyl POSS (which is the sole contributor to the  $-CF_2-$  peak) has a significant surface presence. The tapping-mode AFM phase image presented in Figure 5b is also consistent with this XPS analysis. The bright regions in this micrograph represent fluorodecyl POSS aggregates that have bloomed to the surface during the spin coating and solvent evaporation process (76). Presumably these fluorodecyl POSS aggregates strongly reduce liquid water wettability and are responsible for the relatively icephobic characteristics of the 80/20 PEMA/fluorodecyl POSS surface.

We believe this 80/20 PEMA/fluorodecyl POSS coating with  $\theta_{\rm rec} = 118.2 \pm 2.4^{\circ}$  (and the other fluorodecyl-POSS containing surfaces with similar values of  $\theta_{\rm rec}$ ) essentially yields the minimum strength of ice adhesion that is attainable by reducing the water wettability of smooth surfaces.

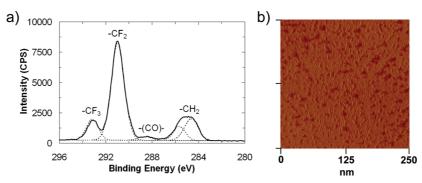


FIGURE 5. Surface characterization of a  $\sim$ 200-300 nm thick layer of 80/20 PEMA/fluorodecyl POSS spin coated onto a silicon wafer. (a) High-resolution carbon 1s X-ray photoelectron spectrum. Peaks corresponding to various carbon moieties located near the surface are labeled. (b) Phase image of a 250 nm  $\times$  250 nm section of the film surface acquired using tapping-mode AFM. The phase angle scale on the image is 0–8°.

It is possible that other attributes of the coatings, such as their viscoelastic properties (27, 30, 31), also influence ice adhesion strength, although the strong correlation presented in Figure 4b implies that these effects are secondary compared to the receding water contact angle parameter  $[1 + \cos \theta_{\rm rec}]$ , at least for the coatings investigated here. The fit to our data provided in eq 5 suggests that a further appreciable reduction in [1  $+\cos heta_{
m rec}$ ] and thus ice adhesion could only be attained by significantly increasing the receding water contact angle above  $\theta_{\rm rec} \approx 120^{\circ}$ . However, the maximum receding water contact angle attainable on a smooth surface with known materials chemistry is  $heta_{
m rec} pprox$ 120° (76, 86). Given this current upper bound in  $\theta_{\rm rec}$ , it is more likely that further significant reductions in ice adhesion strength will be brought about by incorporating microscale and/or nanoscale texture into surfaces. Effective icephobic surfaces will likely allow water droplets to freeze while in the composite (Cassie-Baxter) state, with a reduction in the substrate—ice interfacial area (and possibly the ice adhesion strength) because of the air trapped beneath the ice. The quantitative data recently reported by Kulinich and Farzaneh (53) and Dotan et al. (51) on textured surfaces can be used to evaluate the validity of this prediction. The low stresses of ice detachment reported by these groups were attributed to water droplets freezing in the composite state (51, 53). (A few other groups also investigated ice adhesion on textured surfaces, but did not report the ice adhesion strengths and/or  $heta_{
m rec}$  values needed for inclusion in the compilation (50, 52, 55-58).) The Kulinich and Farzaneh (53) and Dotan et al. (51) data are plotted along with both our data and the best fit to our data in Figure 6. Given that measured values of adhesion strengths are generally sensitive to the specific details of test configurations and conditions (68), the reported data are in good quantitative agreement with the predicted correlation provided in eq 5. Additional efforts aimed at preparing micro- and nanotextured icephobic surfaces with very large receding water contact angles are currently underway in our laboratory.

## **CONCLUSIONS**

The average strengths of ice adhesion were measured on bare steel discs and discs coated with twenty-one different materials with a range of liquid water wettabilities. These

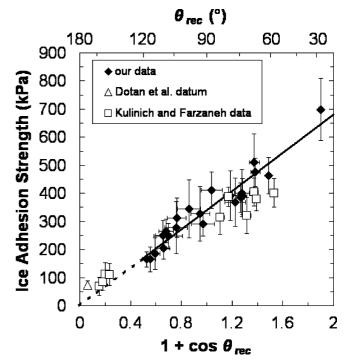


FIGURE 6. Compilation of average strengths of ice adhesion measured in this work (22 nominally smooth test substrates at -10 °C,  $\spadesuit$ ), by Kulinich and Farzaneh (53) (10 textured test substrates at -10 °C,  $\Box$ ), and by Dotan et al. (51) (one textured test substrate at -8 °C,  $\Delta$ ). The solid and dashed lines represent the linear best fit to our data. (predicted average strength of ice adhesion  $\tau_{\rm ice} = (340 \pm 40 \ {\rm kPa})(1 + \cos\theta_{\rm rec})$ ,  $R^2 = 0.92$ ).

measured ice adhesion strengths were compared to different goniometric measures of water wettability that can be used to describe the interactions of the substrates with liquid water and that scale respectively with liquid drop roll-off angle ([cos  $\theta_{\rm rec}$  — cos  $\theta_{\rm adv}$ ], eq 1), equilibrium work of adhesion ([1 + cos  $\bar{\theta}_{\rm e}$ ], eq 2), and practical work of adhesion ([1 + cos  $\theta_{\rm rec}$ ], eq 3) (61, 62). A strong correlation was found between our measurements of the average strength of ice adhesion and the practical work of adhesion scaling parameter [1 + cos  $\theta_{\rm rec}$ ] for liquid water, suggesting that the "icephobicity" of nominally smooth surfaces can be predicted simply by measuring the receding contact angle for water droplets on the substrate (see eq 5). We believe that the fluorodecyl POSS-containing coatings described here have nearly reached the attainable limit of icephobicity for

smooth surfaces, as no known materials have receding water contact angles that are significantly above the  $\theta_{\rm rec}=118.2\,\pm\,2.4^{\circ}$  measured on the 80/20 PEMA/fluorodecyl POSS coating (76, 86). Further reductions in ice adhesion strengths will therefore likely require manipulation of surface texture (e.g., micro- and nanotextures and/or hybrid hydrophilic/hydrophobic surfaces (87)) to enable incident water drops to freeze in the composite (Cassie–Baxter) state.

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Supporting Information Available: Measured surface roughness parameters for the 22 test substrates, a representation of the surface topography of a bare steel disc acquired using a Zygo interferometer, a photograph of the ice adhesion test apparatus, a plot containing Kulinich and Farzaneh's reported ice adhesion strengths (53) as a function of [1 + cos  $\theta_{\rm rec}$ ], plots of measured ice adhesion strength versus [ $\theta_{\rm adv} - \theta_{\rm rec}$ ],  $\theta_{\rm rec}$ , and [1 + cos  $\theta_{\rm adv}$ ], plots of ice adhesion strength as a function of incident probe speed and temperature for four test samples, and SEM and AFM images obtained from silicon wafers coated with fluorodecyl POSS and 80/20 PEMA/POSS (PDF). This material is available free of charge via the Internet at http://pubs.acs.org.

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